

On the use of sub-mesoscale tracer information for the improvement of altimetry-derived velocity fields

A Data Assimilation strategy

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Motivations

- Use of all sort of (satellite) data, mix different scales, physics and biogeochemistry, ...
- Think Data Assimilation accordingly
- **A way to improve our knowledge of ocean currents ?**

Submesoscales ?

- A large range of scales between the mesoscales (≈ 100 km) and the dissipative scales (≈ 1 cm) that seem quite energetic and that we do not know much about ...

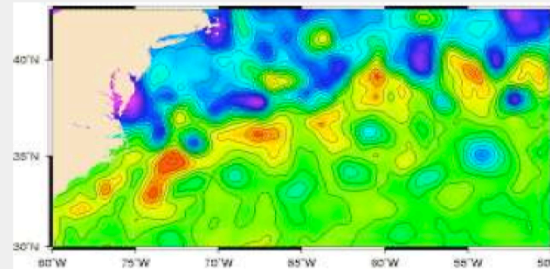


basin scale

Sverdrup balance

$$Ro \approx 10^{-3}$$

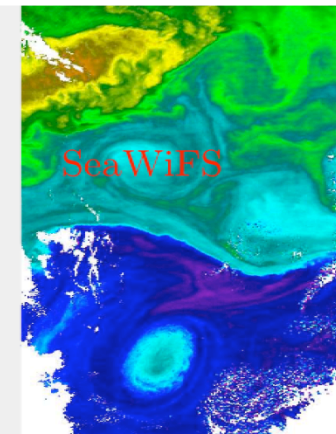
AVISO altimetry



“mesoscale” (synoptic scale)

QG, PE (hydrostatic)

$$Ro \approx .5$$



submesoscale

Navier-Stokes Eq.

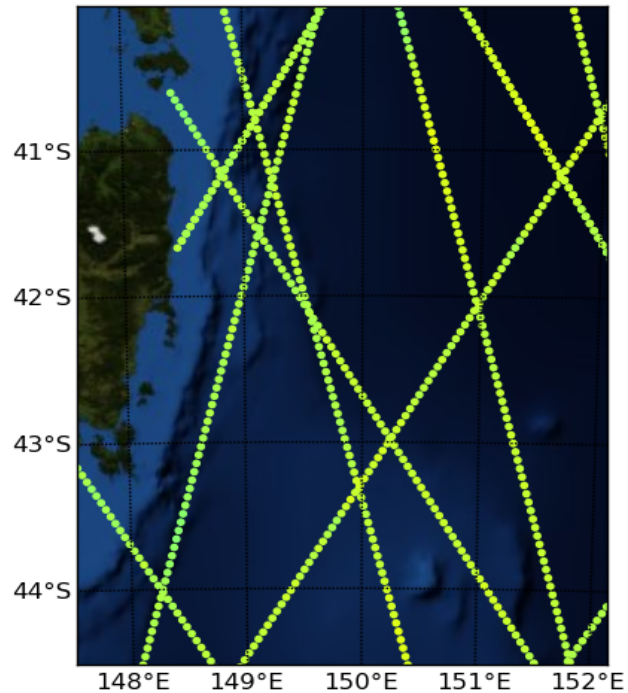
$$Ro > 1$$

1980

2005

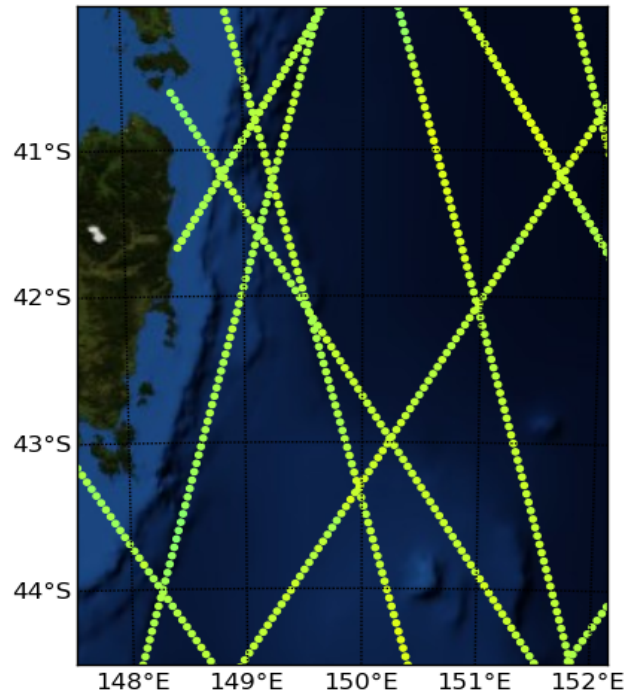
Observations of submesoscales

Submesoscales are not resolved by synoptical observations

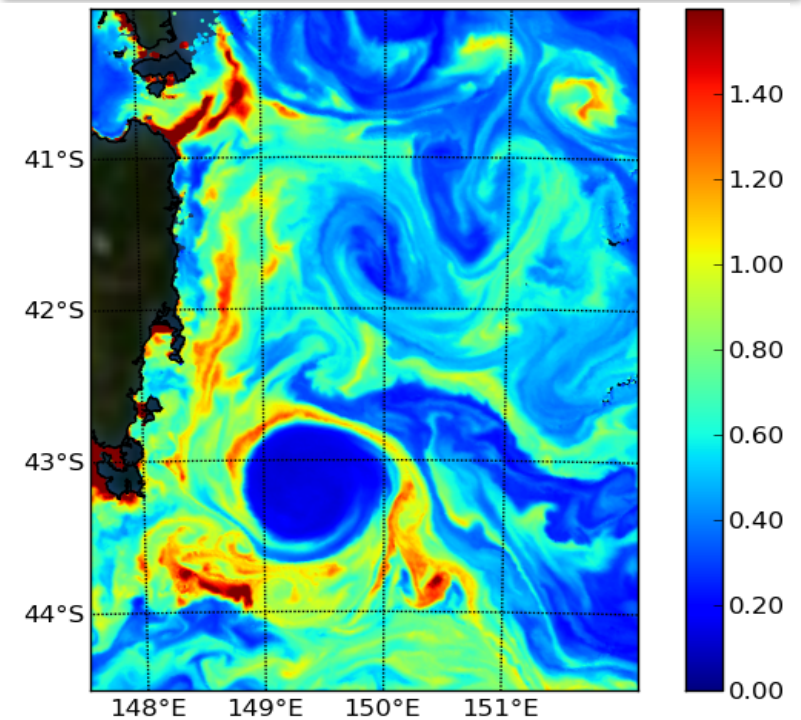


Observations of submesoscales

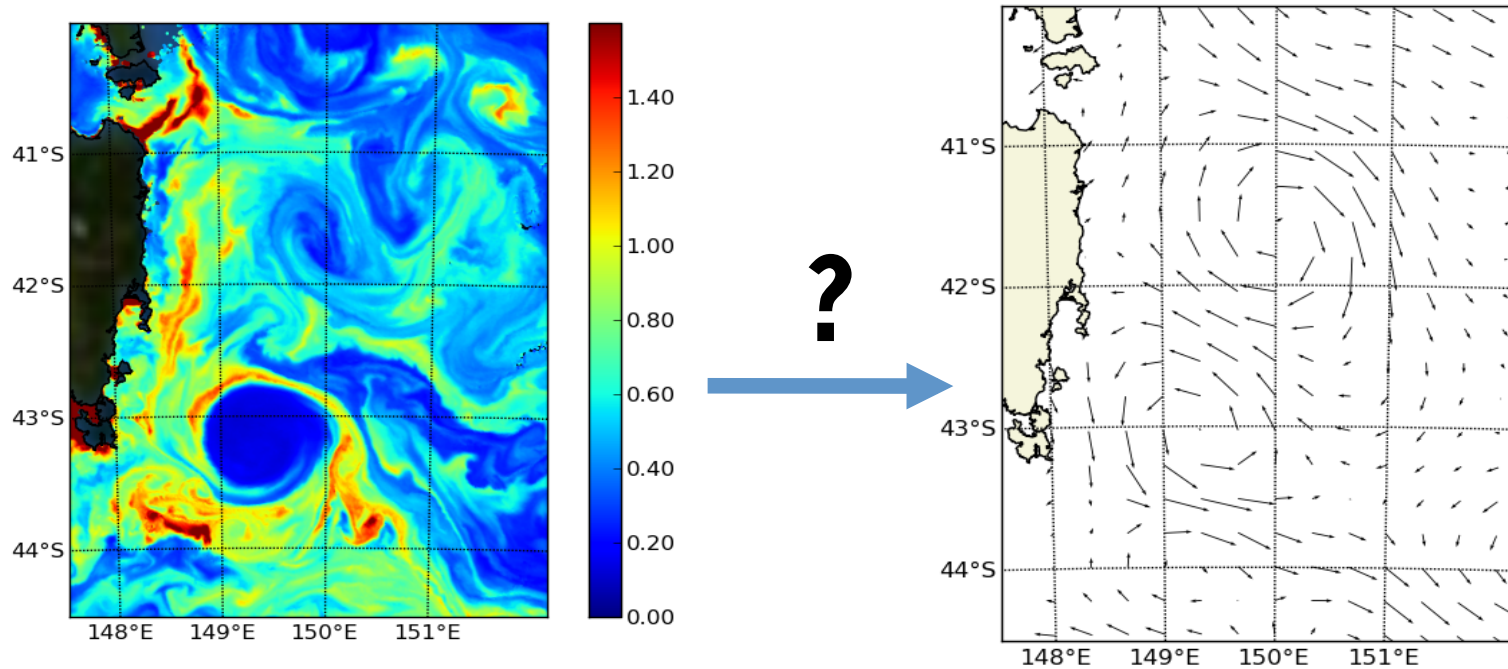
Submesoscales are not resolved by synoptical observations



Submesoscales are observed with satellite tracer sensors



Question: altimetry and high resolution tracer observations

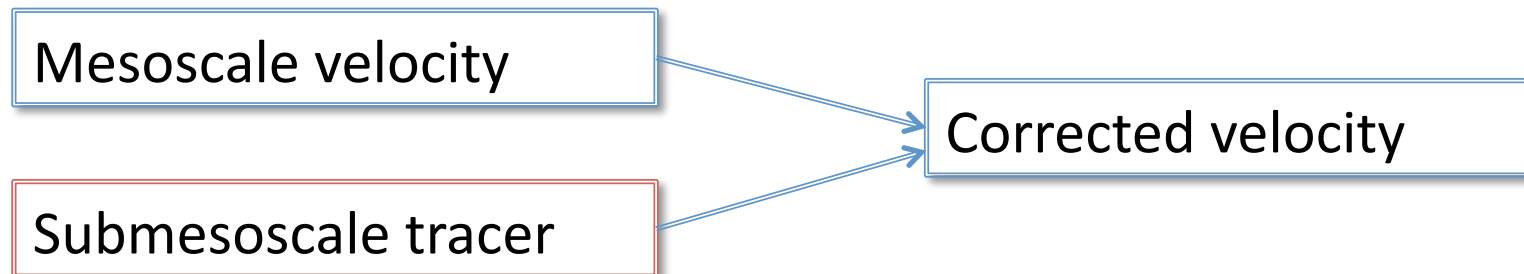


- Is the use of submesoscale tracer information to correct for the mesoscale velocity field feasible ?

Outline

- **Method**
 - A proxy between tracer and velocity
 - Inversion of submesoscale information
- **A Test case**
 - Cost function
 - Corrected velocity field
- **Conclusions**

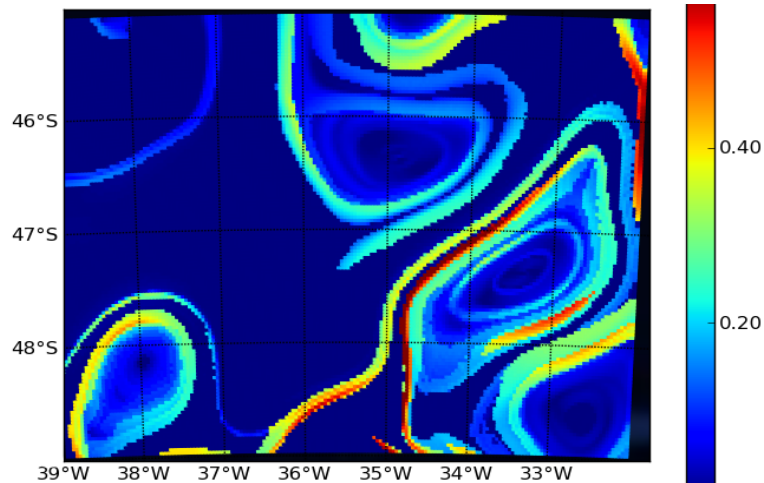
Find a proxy between tracer and velocity



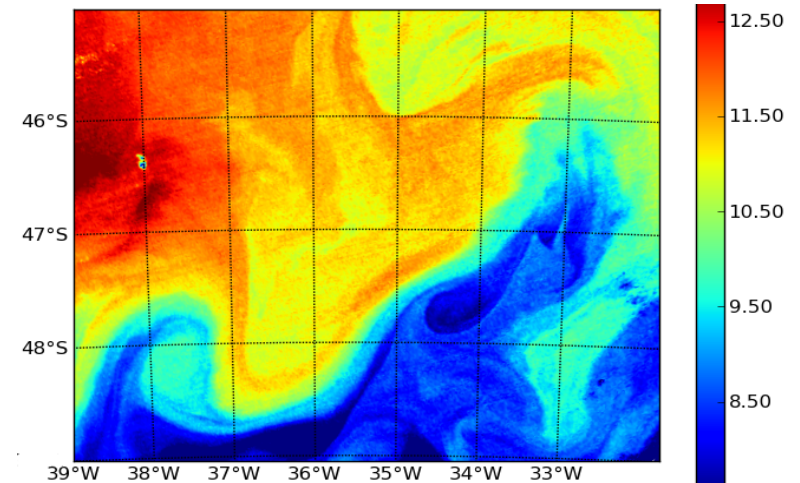
Find the correction the most compatible with tracer information

- The direct measure of the distance between \mathbf{u} and **Tracer** is not possible
- Need to find a go-between variable
- Use of Finite-Size Lyapunov Exponents as a proxy (FSLE)

Lyapunov exponents as a (reliable ?) proxy



FSLE, South Atlantic, Dec 28, 2006



SST tracer, South Atlantic, Dec 28, 2006

- Lyapunov measures fluid stirring
- Link between submesoscale dynamics and biologic stirring
- (Lehahn et al., 2008, D'Ovidio et al., 2004)

Methodology

- **Cost function**

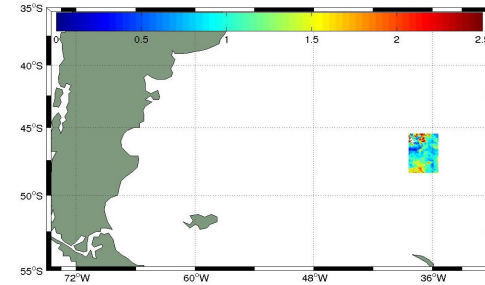
$$J(\mathbf{u}) = \|\mathcal{I}_{\text{FSLE}}(\mathbf{u}) - \mathcal{I}_{\text{OBS}}\| + \text{background term}$$

strongly non-linear cost function with local minima

- Explore subspace errors to find the velocity that minimizes the cost function: using EOFs analysis with all velocity fields available (≈ 100 EOFs used)

$$\mathbf{u}_k = \mathbf{u}_{\text{mean}} + \sum a_k^f \mathbf{u}^f$$

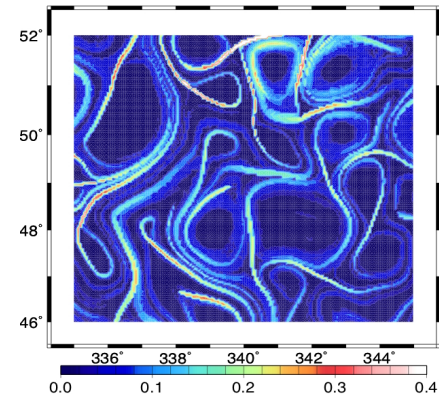
Test case : a small region in the South Atlantic ocean



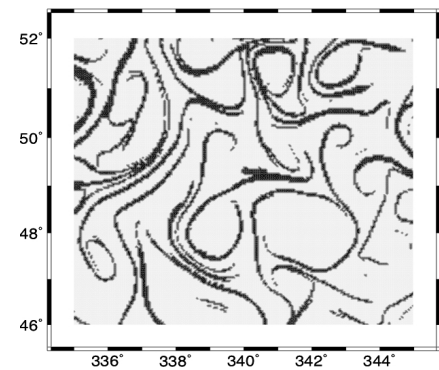
- **Time Range** : from 1998 to June 2009, 595 velocity maps
- **Velocity field** : AVISO, Altimetric data
- **Resolution** : $1/3^\circ$, grid points : $13*17$
- **FSLE Resolution** : $1/48^\circ$, grid points : $99*130$
- **Tracer field** : SST or Chlorophyll data (MODIS sensor, L2 product)
- **Resolution** : $\approx 1/100^\circ$

Transform the Lyapunov exponents into (simple) images

- Observed image structures are extracted using a binarization of the gradient norm
- $Y = 1$ if $\|\delta Y\| > \sigma$
otherwise $Y = 0$
- The threshold σ is chosen such a given percentage of pixels are kept (80%)



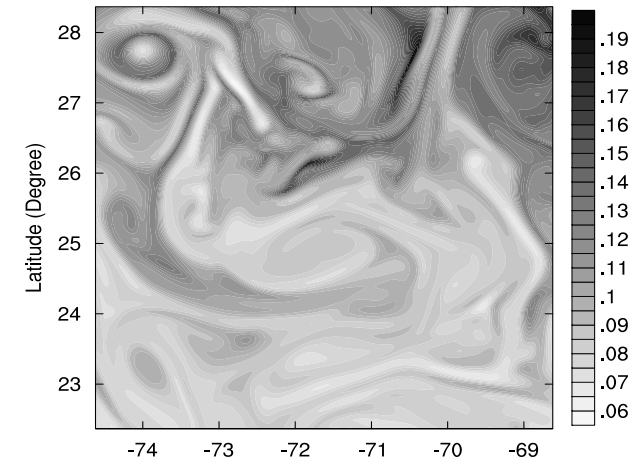
$\|\delta FSLE\|$



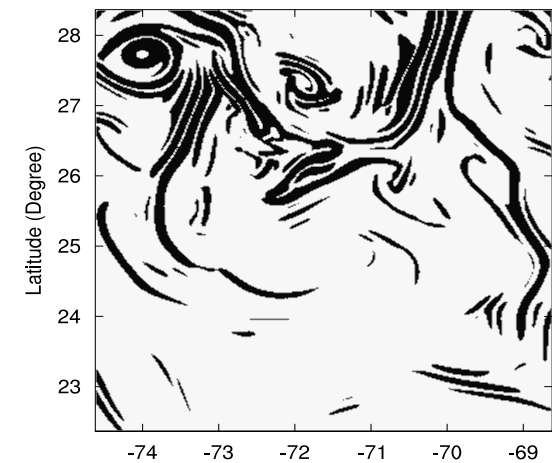
Skeleton image

Generation of phytoplankton (or SST) images

- Observed image structures are extracted using a binarization of the gradient norm
- $Y = 1$ if $\|\delta Y\| > \sigma$ otherwise $Y = 0$
- The threshold σ is chosen such a given percentage of pixels are kept (e. g. 80%)



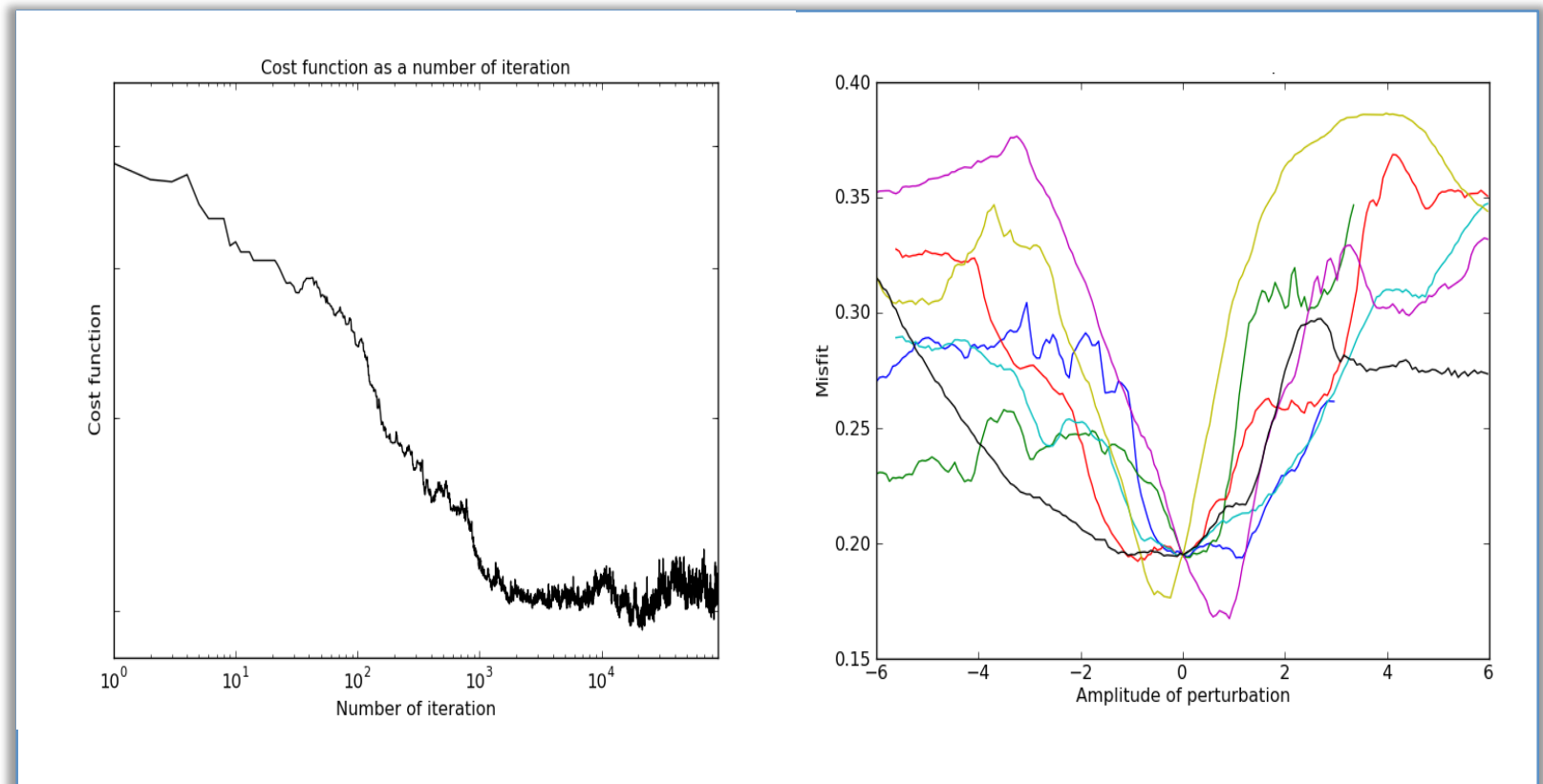
$\|\delta\text{Phytoplankton}\|$



Skeleton image

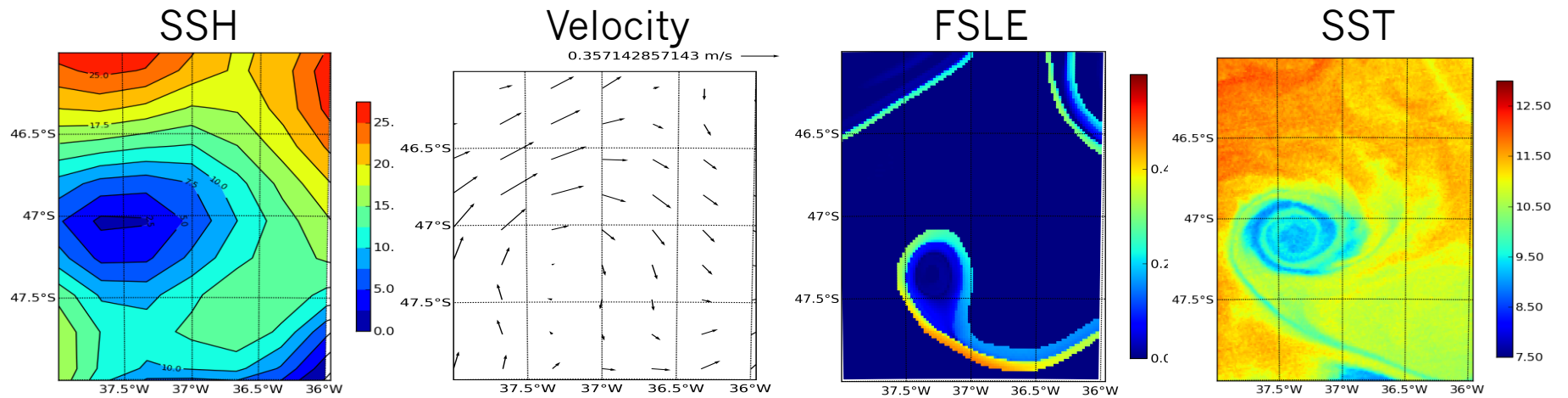
Cost function study: inversion

- Simulated annealing to minimize the cost function
- Gibbs' sampler to get a sample of the potential solutions

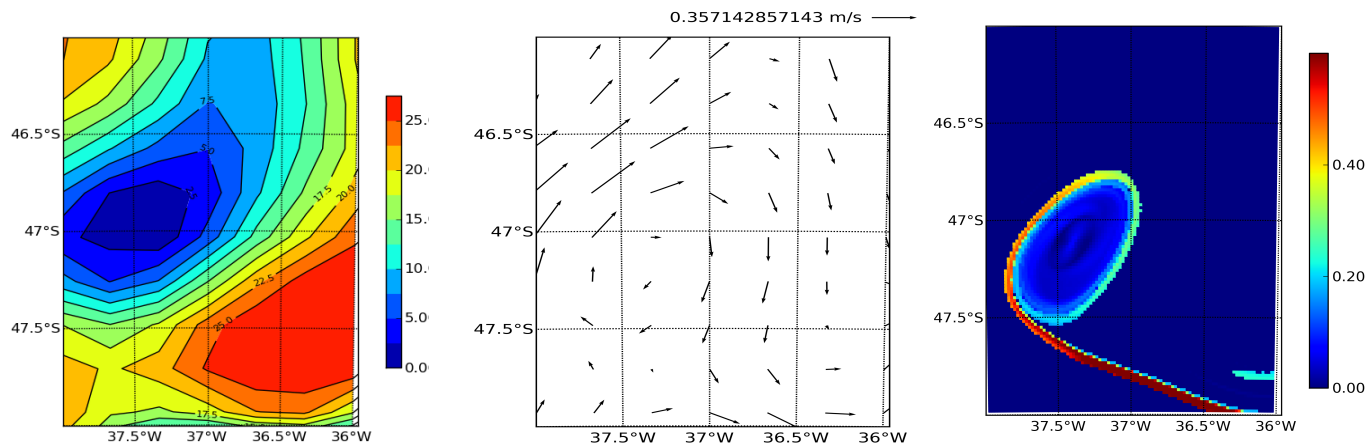


Results: Velocity correction calculated using SST

Observation

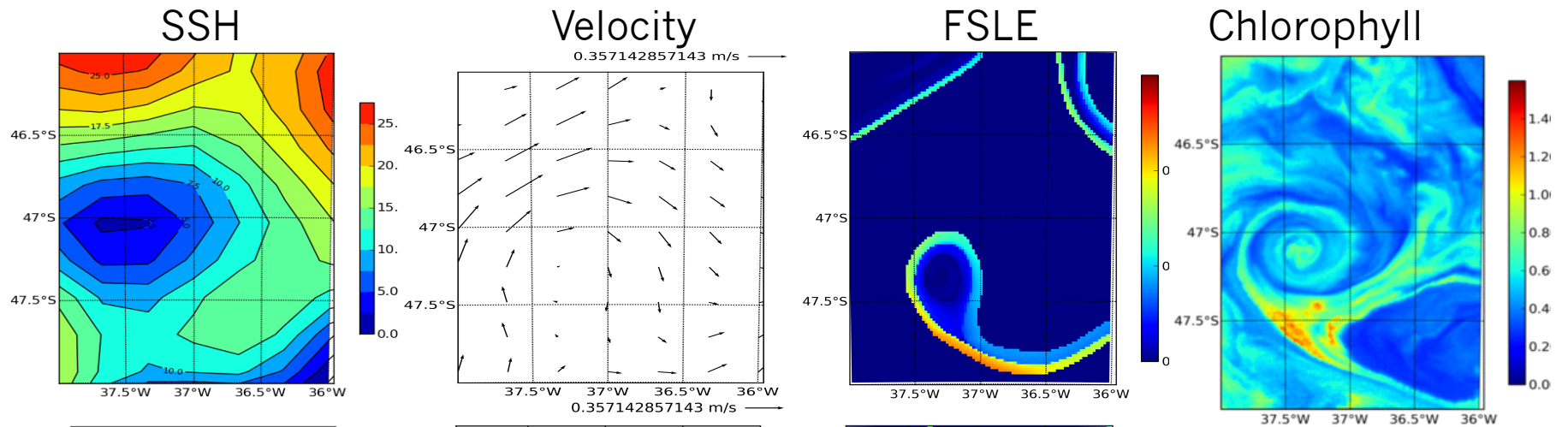


Correction

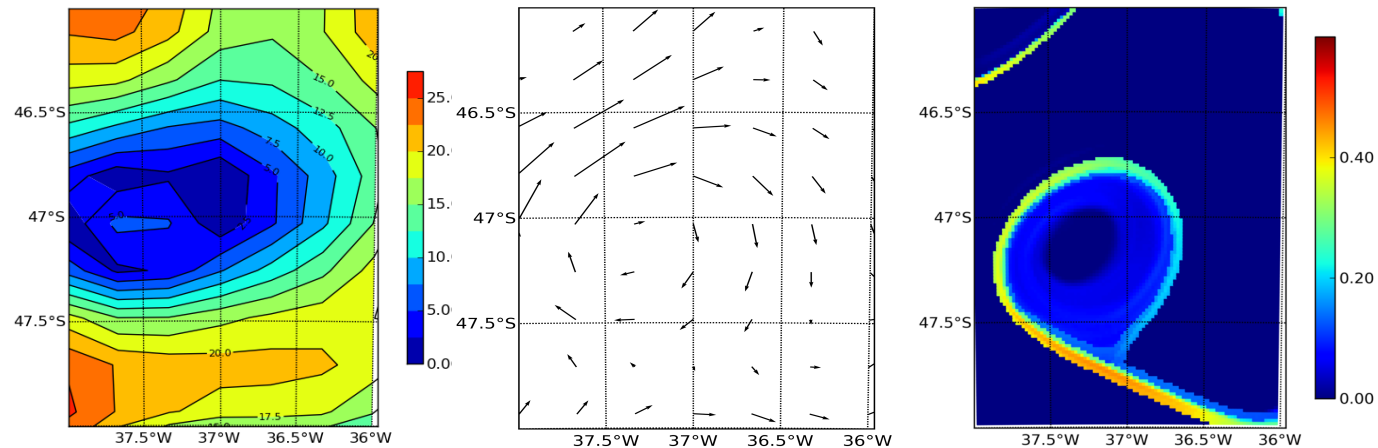


Results: Velocity correction calculated using Chlorophyll

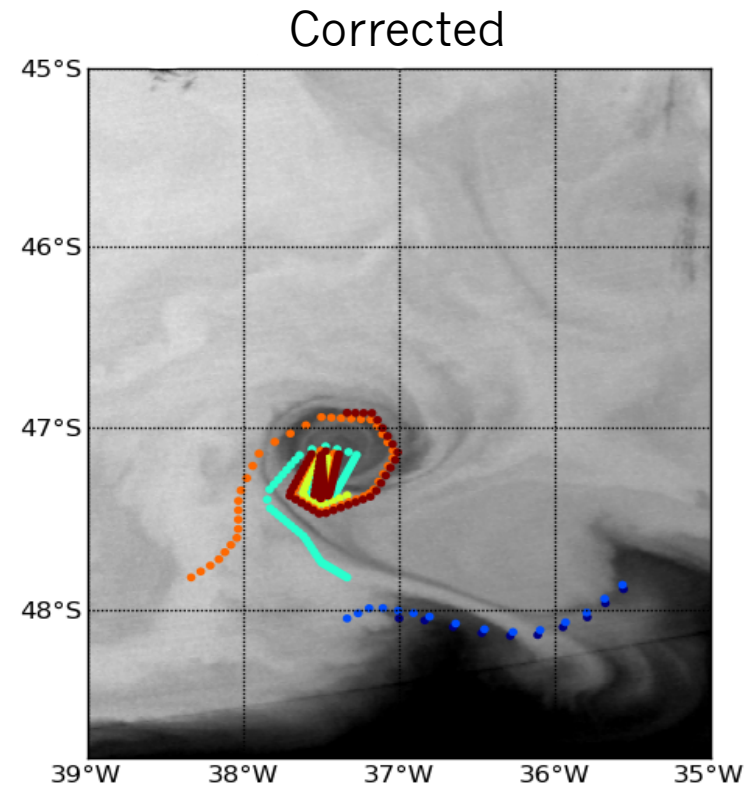
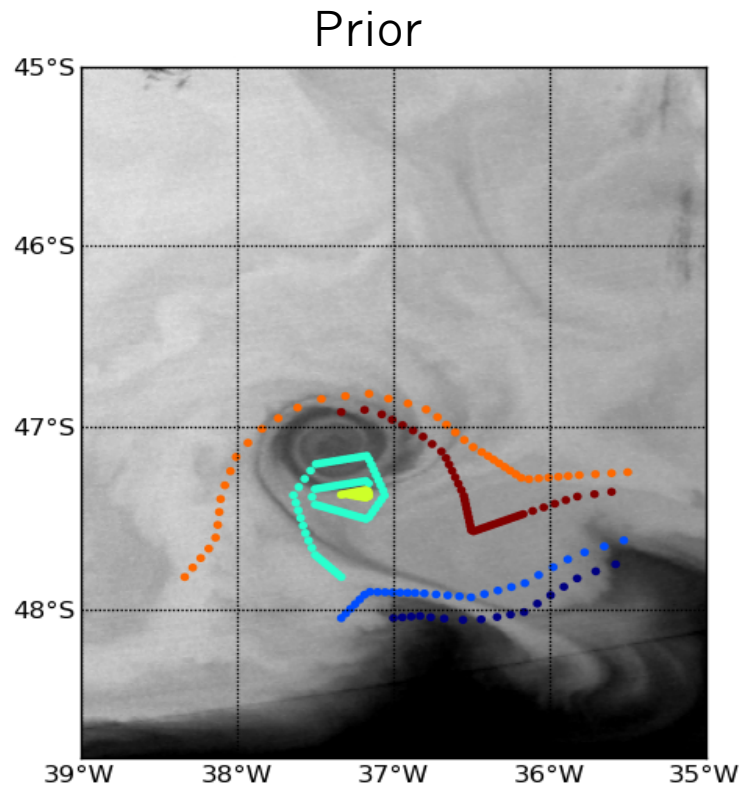
Observation



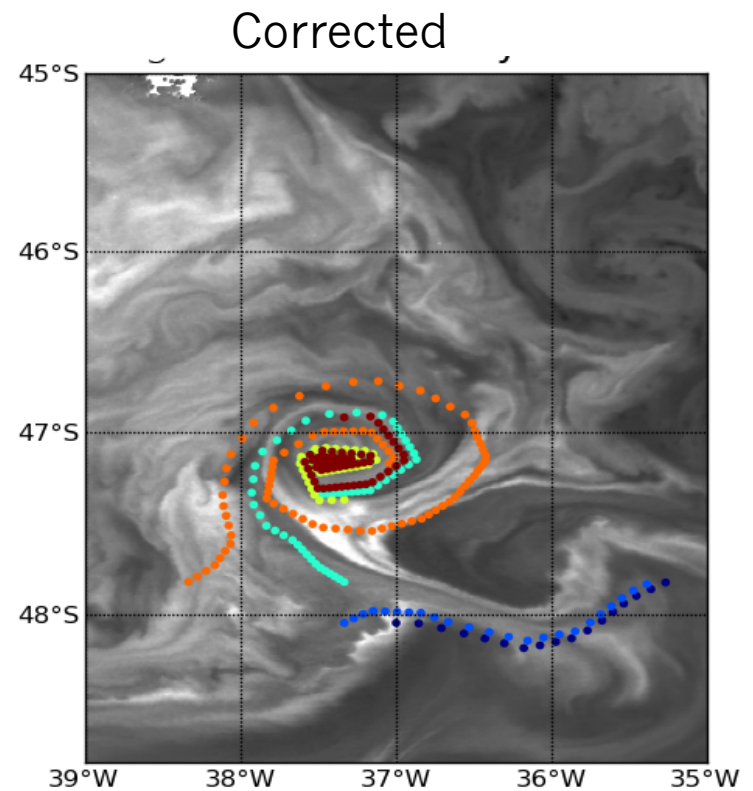
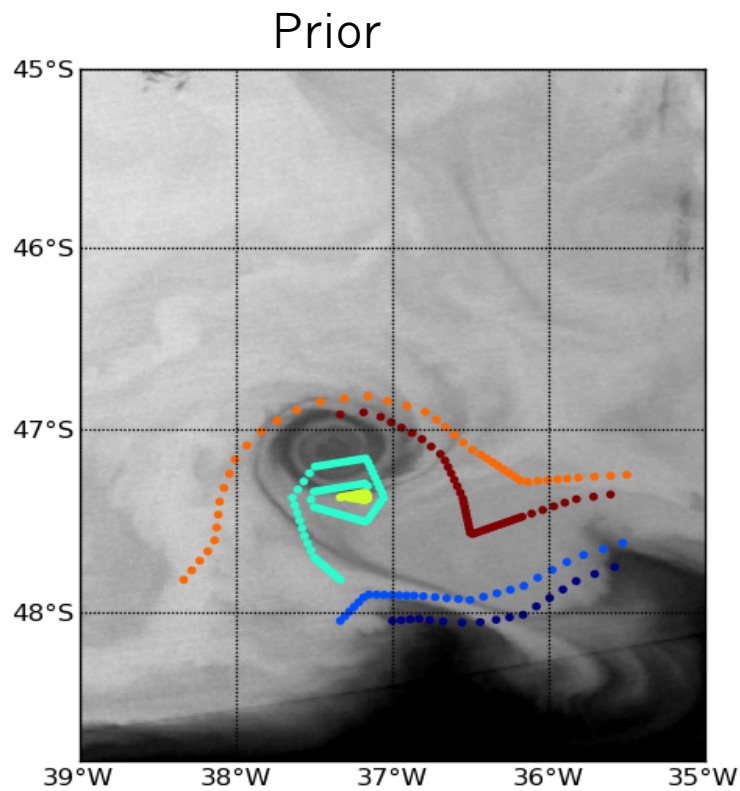
Correction



Results: Lagrangian trajectories / SST tracer



Results: Lagrangian trajectories / Chlorophyll tracer



Conclusion

- Sub-mesoscale information are invertible to control larger scales dynamics
- Altimetry and tracer observations are complementary
- Tracer information can compensate for the lack of SSH resolution in time and space
- High resolution Sea Surface Temperature or Ocean Color data are useful to control ocean physics, in particular ocean currents

Conclusions (cont.)

- Future work
 - Explore joint SST + Chlorophyll inversion
 - Set up an idealized coupled physico-biogeomichal model to assess the submesoscale control in a twin experiment context
 - Full (image + actual data) data assimilation in a coupled model

