

Measuring ocean currents: How far can we go with ESA's Gravity field and steady-state Ocean Circulation Explorer (GOCE) mission?

**Rory Bingham, Newcastle University, UK
rory.bingham@ncl.ac.uk**

Per Knudsen, DTU Space, Denmark

The geodetic method

The geodetic method for estimating geostrophic surface currents:

$$\eta = H - N$$

η , Mean dynamic topography (MDT)

H , Mean sea surface (MSS)

N , Geoid

$$u = -\frac{f}{g} \frac{\partial \eta}{\partial y}, \quad v = \frac{f}{g} \frac{\partial \eta}{\partial x}$$

H, N : $O(100 \text{ m})$

η : $O(1 \text{ m})$

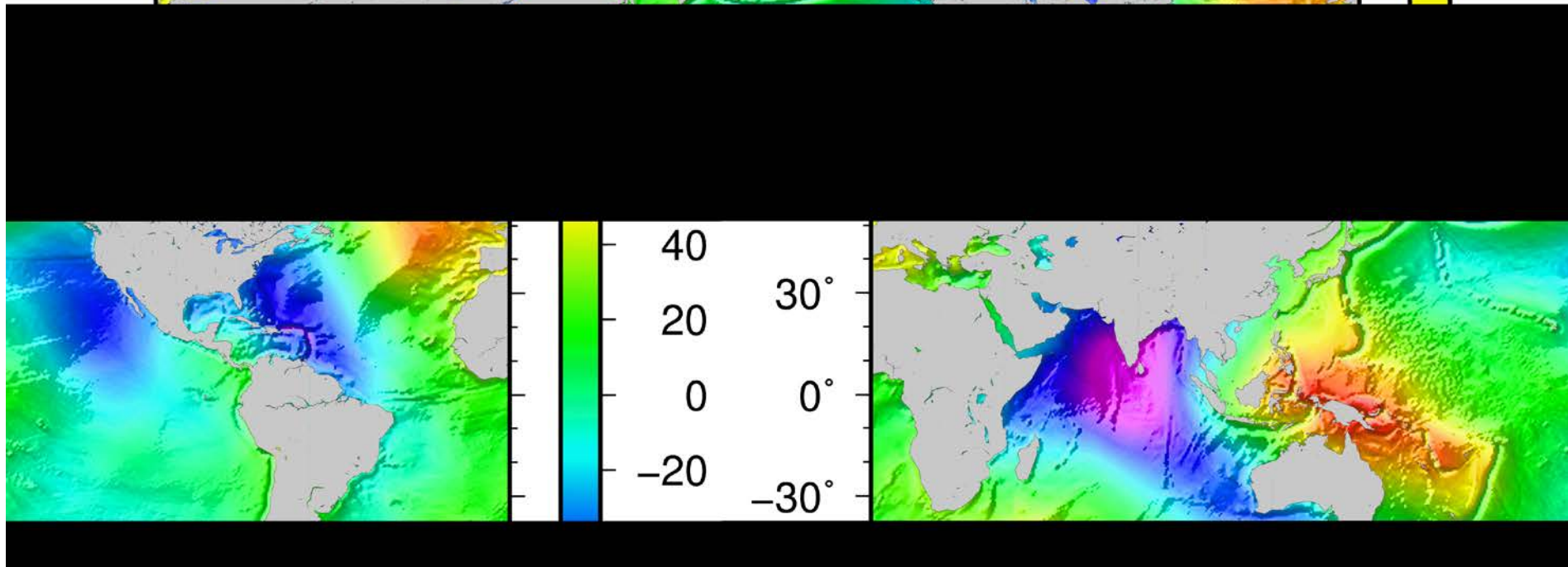
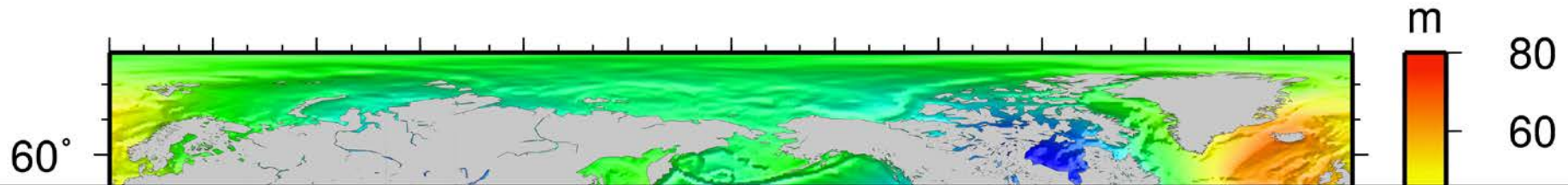
Geoid spherical harmonic model

The mean sea surface

Satellite altimetry provides a beautifully detailed time-mean picture of the ocean's surface

Resolution:
2 arc mins / 2.5 km (mid-latitudes)

Dominated by static-equilibrium response of ocean to Earth's gravity field: The geoid



The time-mean sea surface as measured by satellite altimetry

GOCE: What is it?

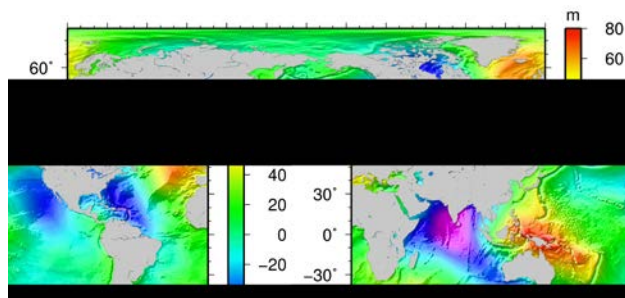
Key features:

- Six three-axis gradiometers
- Low orbit – 254 km
- Ion propulsion – drag free
- Streamlined
- SST and star tracker
- 40 km spacing at equator
- 1 cycle = 61 days = 979 orbits
- Gravity model accuracy < 1cm at 100 km
- Error covariance

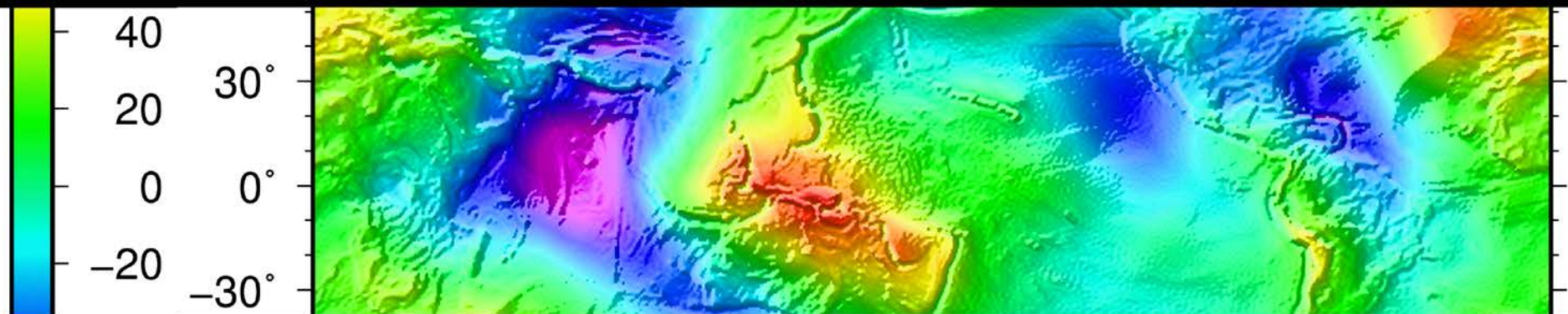
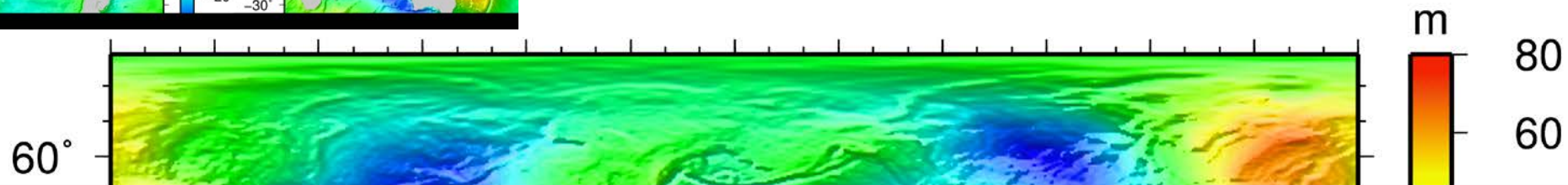
Timeline:

- **17 Mar 09 – launch; alt=283km**
- 20 Mar 09 – early orbit phase completed; SSTI switched on; first science data
- 6 Apr 09 – electronic ion prop engine switched on; alt=280km, decay=190m/day
- 8 Apr 09 – gradiometer on and producing data
- 26 May 09 – drag free op. with ion engine and gradiometer working together
- **30 Sep 09 – in measurement mode and delivering data; alt=255km**
- **30 Jun 10 – First results L2 data – earth gravity models and gradients – released**
- **6 Sep 10 - GOCE recovers from telemetry glitch that had prevented the satellite from sending its scientific data to Earth for several weeks**
- 3 Mar 2011 - Second EGM's released
- 11 Nov 2011 – Third EGM's released

The GOCE geoid

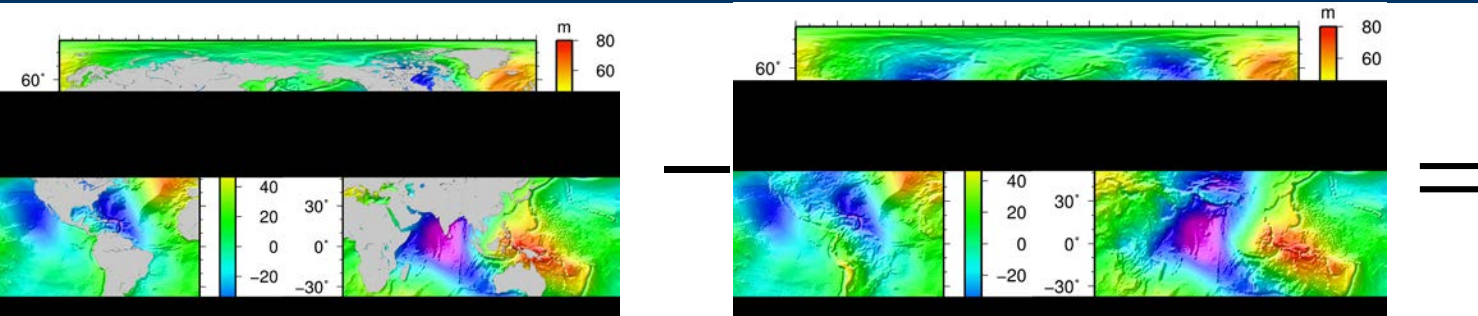


The time-mean sea surface as measured by satellite altimetry

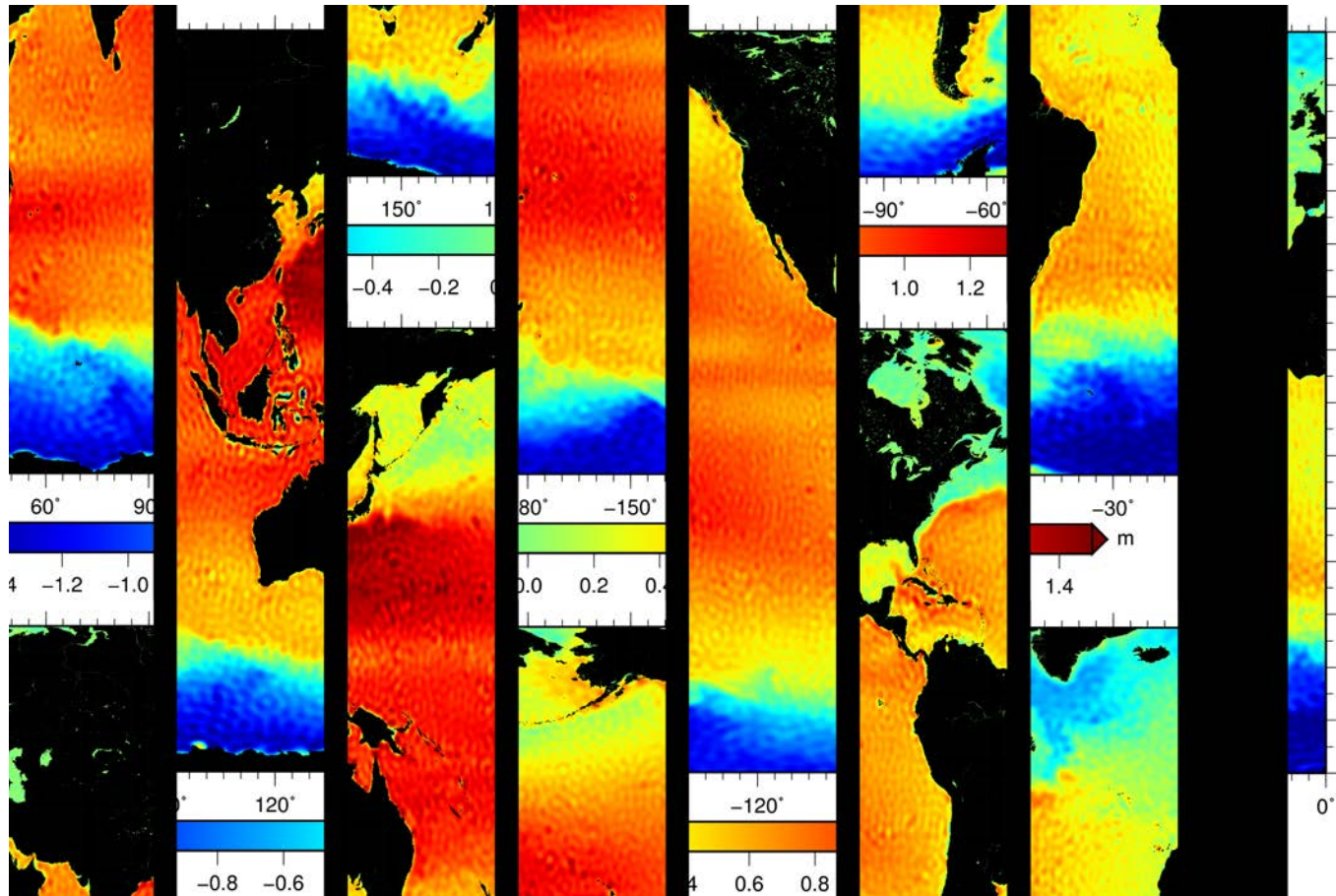


The geoid derived from the 3rd time-wise GOCE gravity model

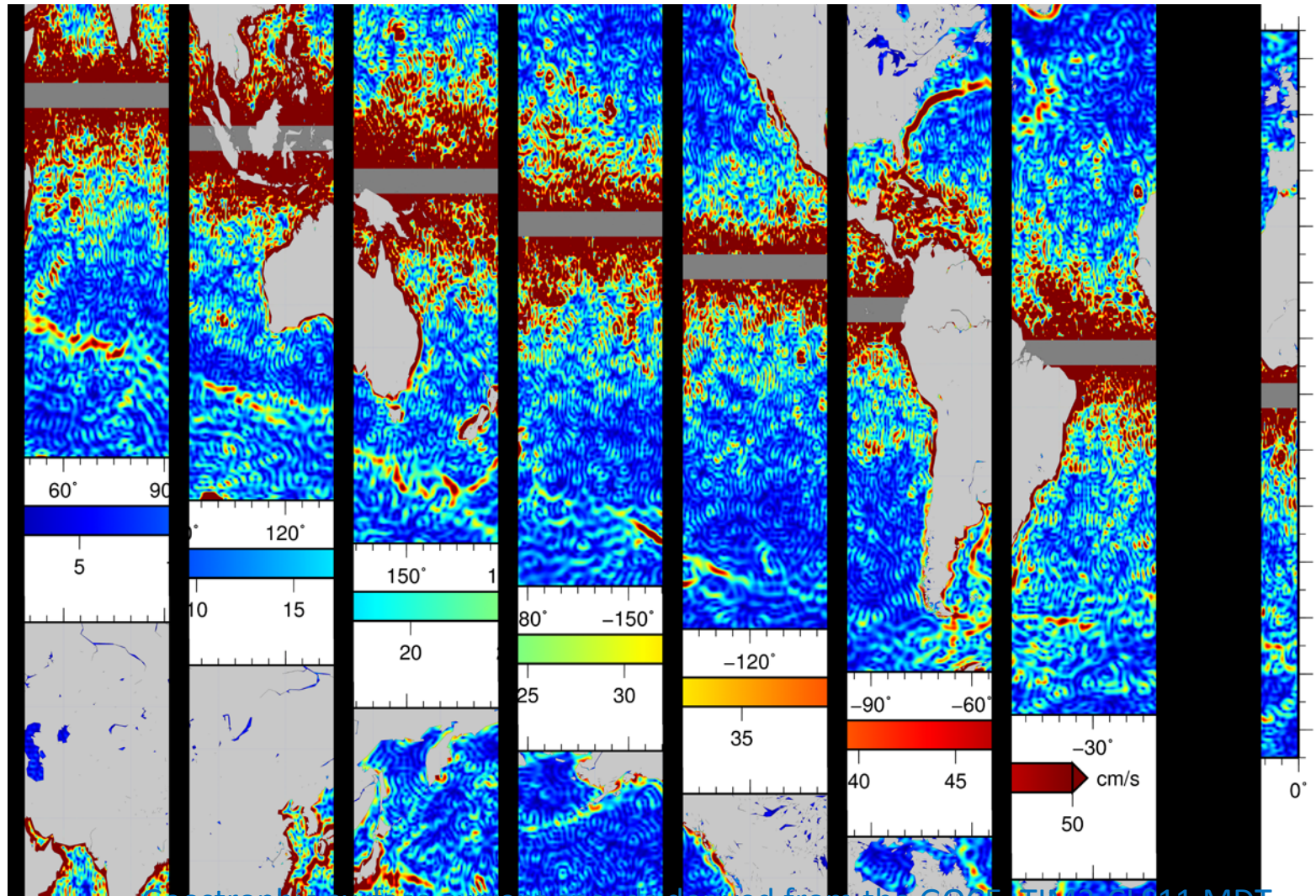
The GOCE mean dynamic topography



Subtracting the geoid from the MSS reveals the ocean's mean dynamic topography (MDT)



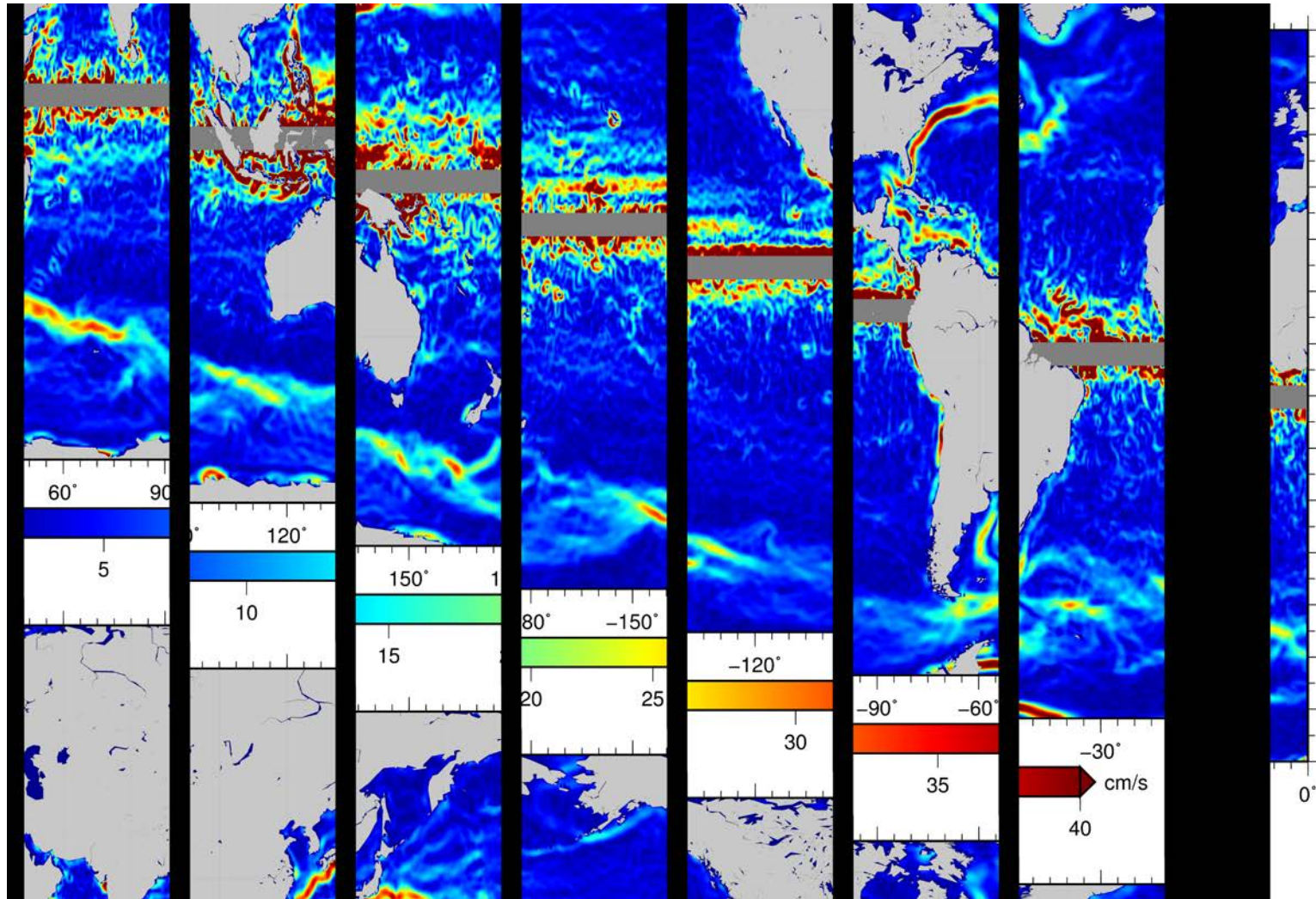
Geostrophic currents from GOCE



Geostrophic surface current speeds derived from the GOCE_TIM3-CLS11 MDT

$$U = \frac{f}{g} \sqrt{\left(\frac{\partial \eta}{\partial x}\right)^2 + \left(\frac{\partial \eta}{\partial y}\right)^2}$$

Geostrophic currents from GOCE



Geostrophic surface current speeds derived from the **filtered** GOCE_TIM3-CLS11 MDT

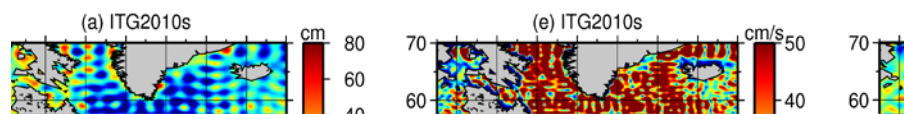
Progress so far: North Atlantic MDT and currents

GRACE (8 yrs)

Comparison at
 $d/o=180$ (111 km)

GOCE (2 mnths)

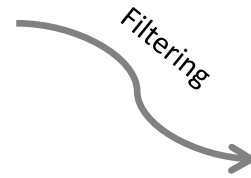
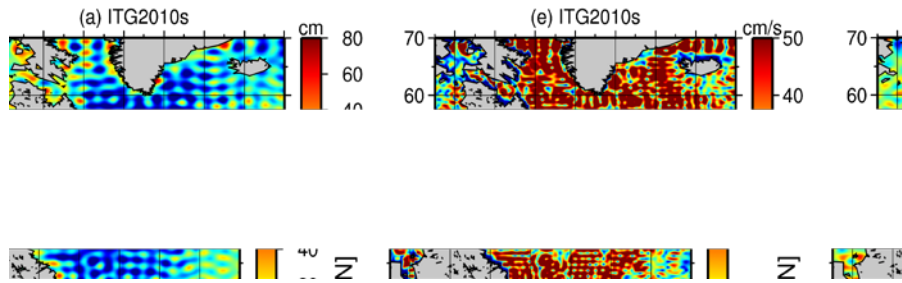
GOCE considerably
less noisy



GOCE (1 yr)

Some filtering still
required

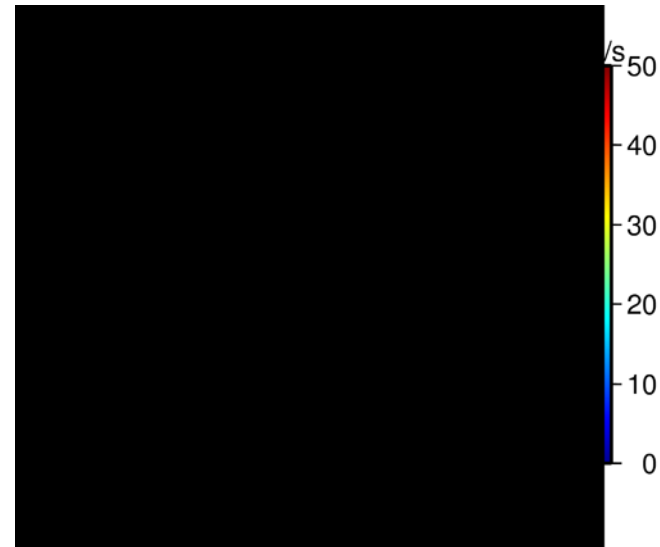
Progress so far: North Atlantic MDT and currents



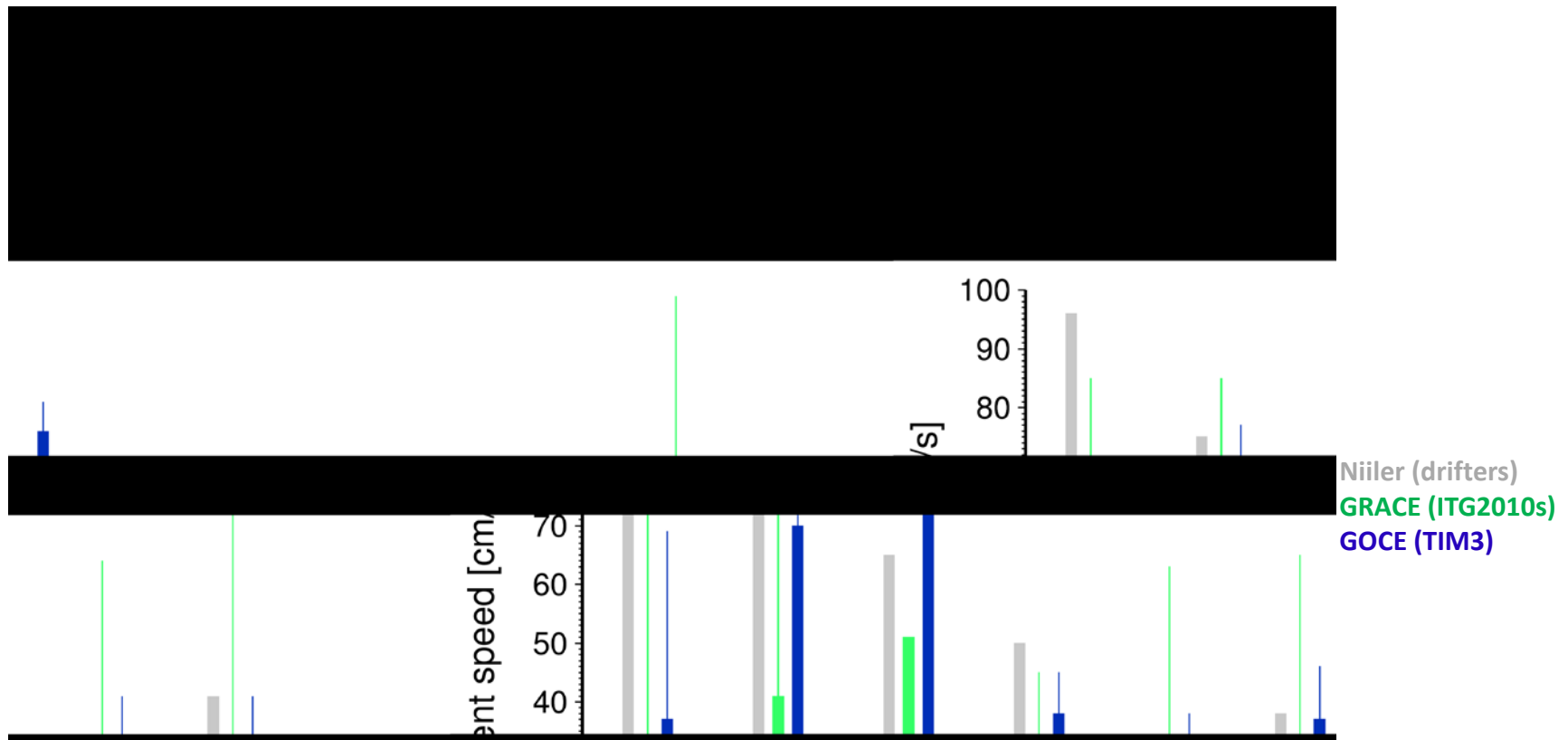
less noise

less filtering

better currents



Progress so far: North Atlantic MDT and currents



A comparison of current speeds at 9 locations in the North Atlantic

GOCE: How far can we go?

- The spatial resolution of GOCE is the limiting factor:

Relationship between spatial res. (S) max degree (L):

$$S = \frac{20000}{L} \text{ km}$$

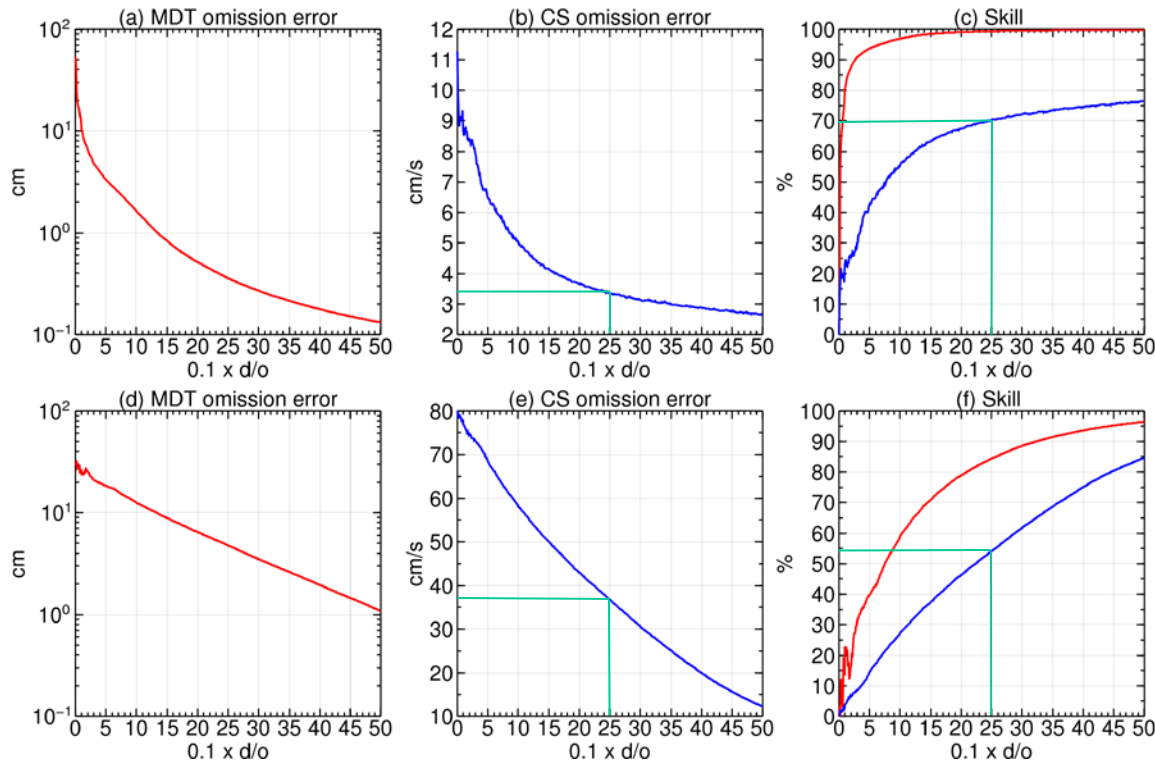
Spatial resolution of GOCE:

$$L = 250 \Rightarrow S = 80 \text{ km}$$

SH degrees in MSS:

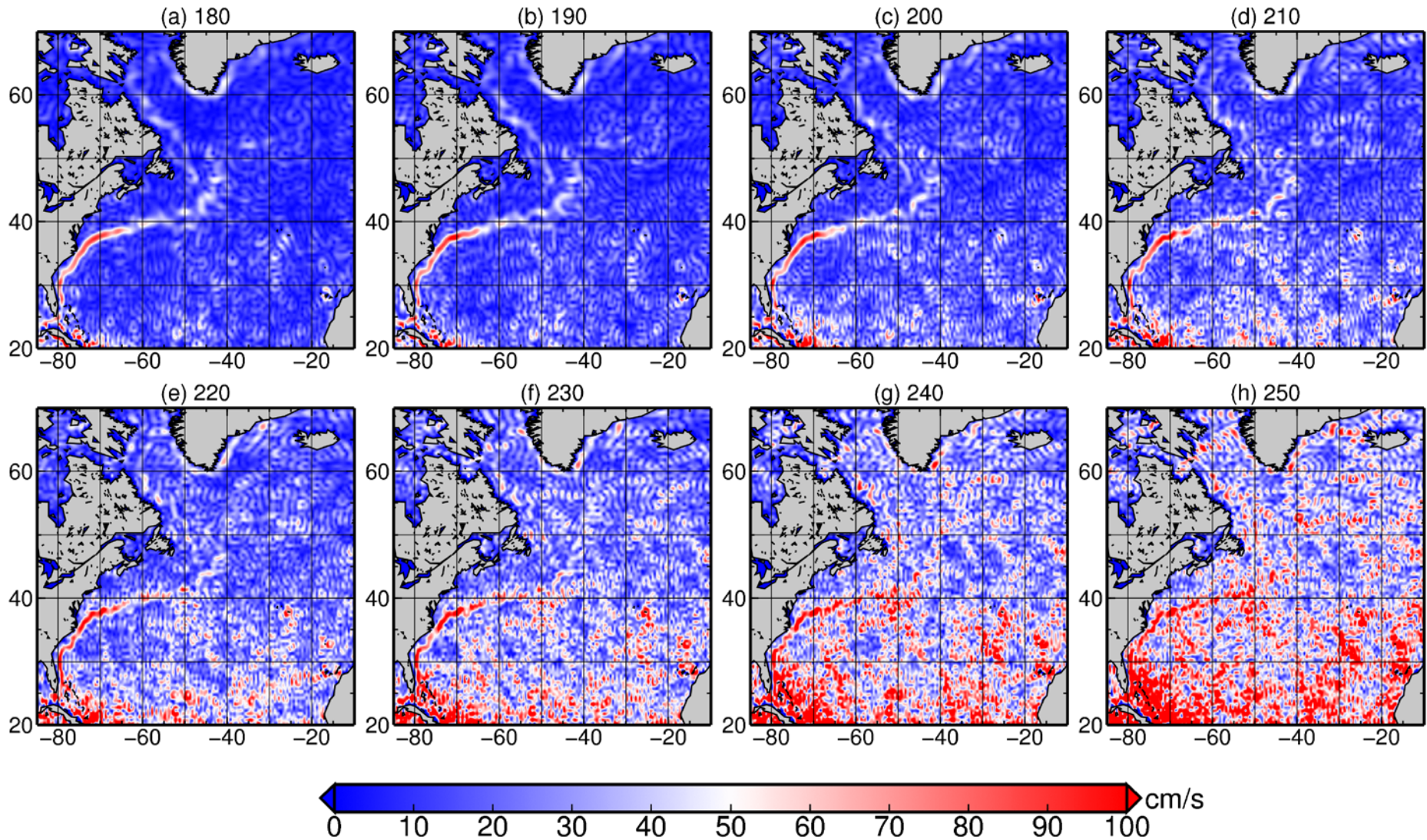
$$S = 5 \text{ km} \Rightarrow L = 4000$$

A model of MDT omission error (1/12th degree OCCAM)



- Currents – high degrees more important
- Particularly for strong currents
- At degree 250, global error:
 - 3 cm/s
 - 70% recovery
- At degree 250, Gulf Stream error:
 - 35 cm/s
 - 55% recovery
- Pessimistic

The issue of geoid commission error



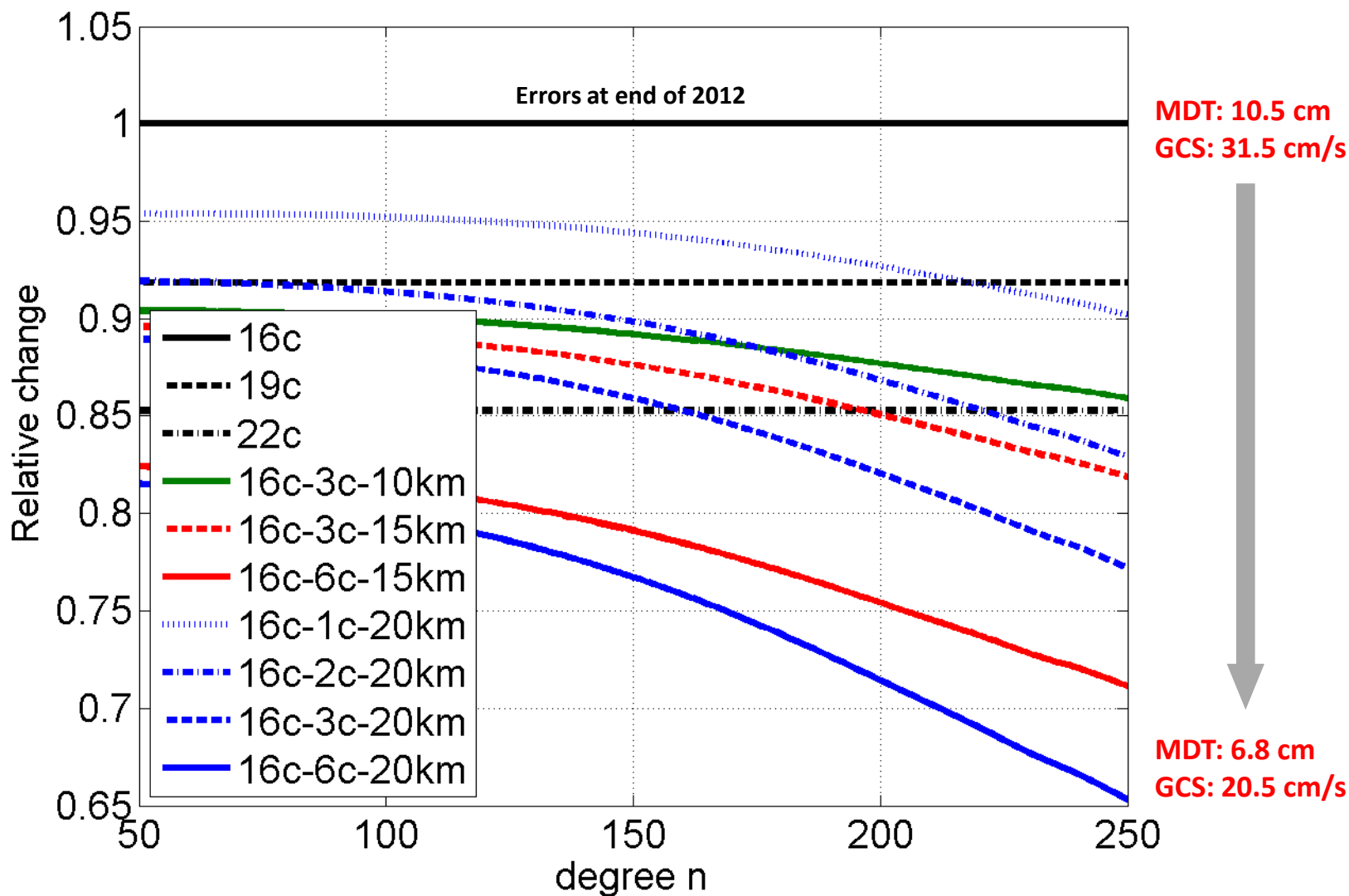
North Atlantic currents speeds obtained from MDTs based on the 3rd timewise GOCE gravity model with increasing MDT truncation from $d/o=180$ to 250.

Realising the potential of GOCE

Realising the full potential of the GOCE mission will depend on how geoid commission errors can be dealt with:

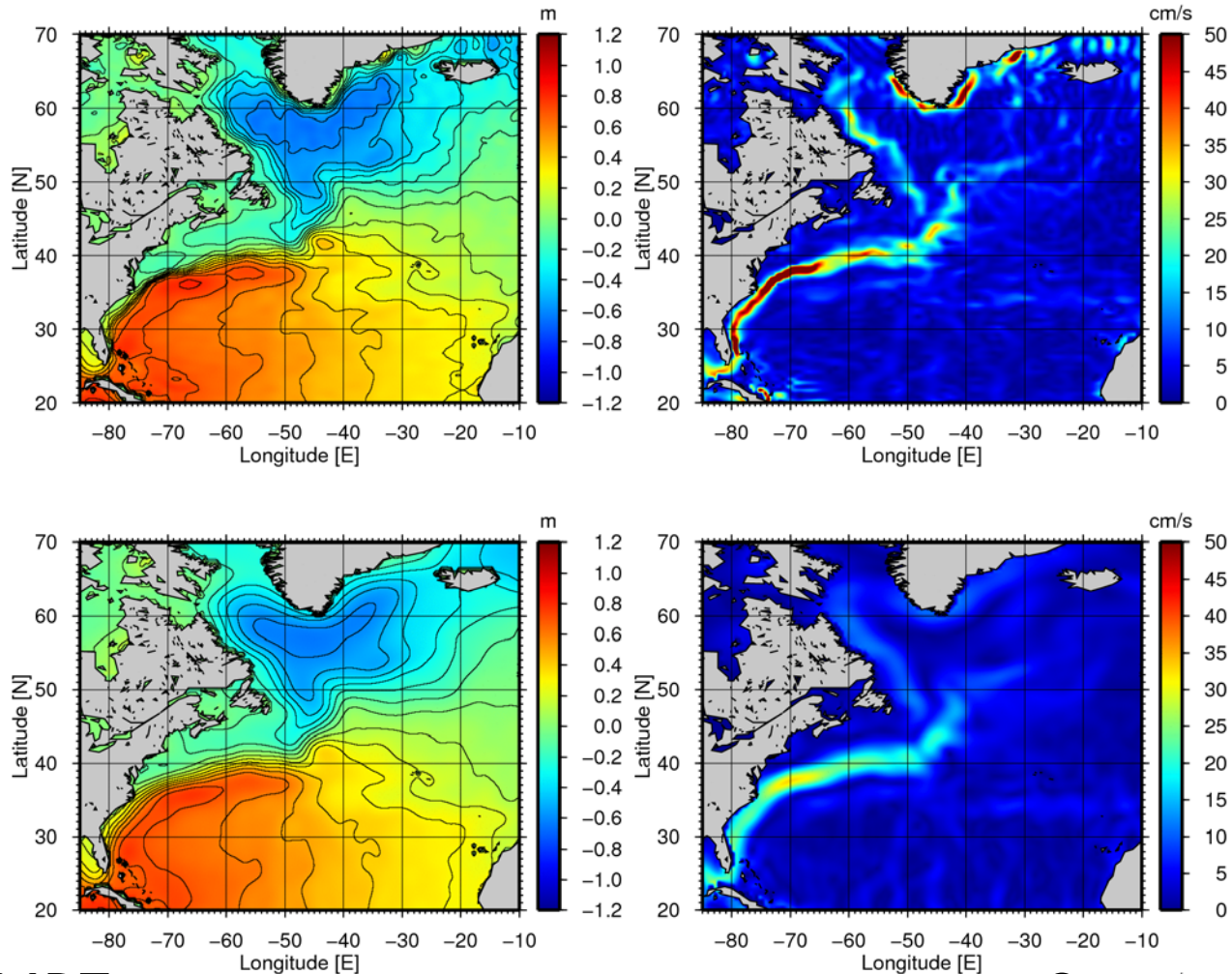
- More data
 - Lower orbit
- } Mission scenarios
- Filtering strategies
 - Data synthesis
- } Post processing

Realising the potential of GOCE: Mission scenarios



Realising the potential of GOCE: Filtering

Diffusive filter



MDTs

Gaussian filter – 150km

Currents

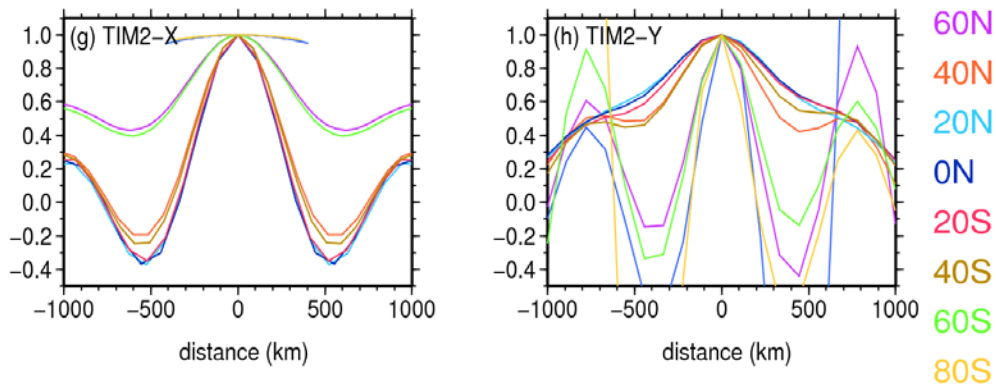
Diffusive filtering effectively removes noise while preserving gradients associated with strong currents

Realising the potential of GOCE: Data synthesis

Formal GOCE geoid/MDT error

- Error variance-covariance
- Formal errors on geoid/MDT
- Error structure
- Optimal filtering
- Rigorous data synthesis
- Data assimilation

Formal GOCE geoid/MDT error covariance (zonal; meridional)



Summary

- Significant improvement over GRACE
- Potential: 80 km
- At least 70% of geostrophic current field captured
- Commission errors – signal to noise ratio:
 - More data
 - 20 km lower in 2013: GSC errors = 20 cm/s
 - More sophisticated filtering: error information; auxiliary data
- GOCE will never provide the meso-scale but:
 - Most accurate at scales resolved
 - Provides foundation
 - Formal error for optimal/rigours blending
- Data assimilation